- 1. (a) FALSE. Existence of inverses; for example, 2^{-1} .
 - (b) FALSE. Must have same operation in group and subgroup.
 - (c) TRUE.
 - (d) FALSE. Odd times odd is even. Alternate: the identity is even.
 - (e) FALSE. Give an example such as $(123)(45) \in S_5$, which has order 6.
- 2. (a) $\alpha = (152)(34)$
 - (b) $|\alpha|$ is the least common of its cycle lengths when in disjoint form; that is, lcm(3,2) = 6.
 - (c) It is odd. The parity is the same as the parity of the number of even cycles.
- 4. (a) Given two elements $X = axa^{-1}$ and $Y = aya^{-1}$ with $x, y \in H$, we have

$$XY^{-1} = axa^{-1}(aya^{-1})^{-1} = axa^{-1}(ay^{-1}a^{-1}) = a(xy^{-1})a^{-1}.$$

This is in aHa^{-1} since $xy^{-1} \in H$ because H is a group.

(b) $\varphi(x)\varphi(y) = axa^{-1}aya^{-1} = axya^{-1} = \varphi(xy).$