## Math 274 Final

December 13, 2013

- Please put your name, ID number, and sign and date.
- There are 2 problems worth a total of 50 points.
- You must show your work to receive credit.

Print Name: $\qquad$

Student ID: $\qquad$

Signature and Date: $\qquad$

| Problem | Score |
| :---: | :---: |
| 1 | $/ 25$ |
| 2 | $/ 25$ |
| Total | $/ 50$ |

1. $(25 \mathrm{pts})$ Let $A$ be an $n \times n$ symmetric matrix. Let $B=\left(b_{i j}\right)$ denote the results of $A$ after one step of Gaussian elimination (so $b_{i 1}=0$ for $i=2, \ldots, n$ ). Prove $b_{i j}=b_{j i}$ for all $i, j=2, \ldots, n$.
2. ( 25 pts ) Prove the uniqueness of polynomials of degree $\leq 3$ satisfying

| $x$ | $x_{0}$ | $x_{1}$ |
| :---: | :---: | :---: |
| $f(x)$ | $y_{0}$ | $y_{1}$ |
| $f^{\prime}(x)$ | $z_{0}$ | $z_{1}$ |

when $x_{0} \neq x_{1}$.

