(1) Prove Theorems 5.7, 5.8, and 5.10 in the book.
(2) Do problem 4.5.
(3) Do problem 4.7.
(4) Do Problem 5.3.
(5) Let $f(n, k)$ be the number of ways of arranging $n$ children in a circles such that each circle consists of at least 2 children holding hands and there is child in the center of each circle. Find the generating function

$$
1+\sum_{n \geq 3} \frac{t^{n}}{n!} \sum_{k \geq 1} f(n, k) x^{k}
$$

