

*Department of Mathematics,  
University of California, San Diego*

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# University of California Lie Theory Workshop

**Prof. Vera Serganova**

University of California, Berkeley

## On the category of bounded $(g, k)$ -modules

### Abstract:

This talk is based on my joint work with I. Penkov. Let  $g$  be a simple Lie algebra, and  $k$  be a reductive subalgebra in  $g$ . A  $(g, k)$ -module  $M$  is bounded if it is locally finite over  $k$  and the multiplicities of all irreducible finite-dimensional modules in  $M$  are uniformly bounded. (Two examples from classical representation theory are ladder modules in Harish-Chandra theory and cuspidal modules in case when  $k$  is a Cartan subalgebra).

I will formulate several general results about bounded modules involving primitive ideals theory and geometry (localization). Then I concentrate on the example when  $g = B_2$ , and  $k$  is the principal  $sl(2)$ -subalgebra, where the complete classification of irreducible simple bounded  $(g, k)$ -modules is done.

Host: Efim Zelmanov

**Saturday, February 16, 2008**

**11:10 AM**

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