## Math 10B



University of California, San Diego Department of Mathematics

Instructions

- 1. Write your Name, PID, Section, and Exam Version on the front of your Blue Book.
- 2. No calculators or other electronic devices are allowed during this exam.
- 3. You may use one page of notes, but no books or other assistance during this exam.
- 4. Write your solutions clearly in your Blue Book.
  - (a) Carefully indicate the number and letter of each question and question part.
  - (b) Present your answers in the same order they appear in the exam.
  - (c) Start each problem on a new page.
- 5. Show all of your work. No credit will be given for unsupported answers.
- 6. Turn in your exam paper with your Blue Book.
- 7. NOTE: This exam has two sides.
- 0. (1 point) Carefully read and complete the instructions at the top of this exam sheet and any additional instructions written on the chalkboard during the exam.
- 1. (6 points) A toy rocket flies straight up. After t seconds in the air, the velocity of the rocket is v(t) feet per second. The value of v(t) for several values of t is given in the table below.

t	0	10	20	30
v(t)	0	1	4	9

- (a) Compute  $L_3$  (the left sum with N = 3).
- (b) Compute  $R_3$  (the right sum with N = 3).
- 2. (18 points) (a) Let f be an odd function such that  $\int_{-2}^{3} f(x) dx = 7$ .

Compute 
$$\int_{2}^{3} \left[ f(x) + 2 \right] dx.$$

(b) Let g be an even function such that  $\int_{-2}^{3} g(x) dx = 5$  and  $\int_{0}^{2} g(x) dx = 2$ . Compute  $\int_{0}^{3} \left[ g(x) + 1 \right] dx$ .

Compute 
$$\int_{2}^{3} \left[ g(x) + 1 \right] dx$$

(c) Find the average value of 2f(x) - g(x) over the interval [2,3].

3. (10 points) The following is the graph of y = f(x).



- (a) Compute  $\int_{0}^{12} f(x) dx$ . (b) If F'(x) = f(x) and F(0) = 15, what is F(12)?
- (c) If F'(x) = f(x) and F(0) = 0, then find one value  $x_0$  in the interval [0, 8] for which  $F(x_0) = 10$ .
- 4. (15 points) Compute the given definite and indefinite integrals.
  - (a)  $\int_0^1 \left(\sqrt{x} 3e^x\right) dx$ <br/>(b)  $\int \left(4\cos(t) 3\right) dt$

(c) 
$$\int \frac{(u^2 - 3)^2}{u} du$$