Math 10B



University of California, San Diego Department of Mathematics

Instructions

- 1. Write your Name, PID, Section, and Exam Version on the front of your Blue Book.
- 2. No calculators or other electronic devices are allowed during this exam.
- 3. You may use one page of notes, but no books or other assistance during this exam.
- 4. Read each question carefully, and answer each question completely.
- 5. Write your solutions clearly in your Blue Book.
 - (a) Carefully indicate the number and letter of each question and question part.
 - (b) Present your answers in the same order they appear in the exam.
 - (c) Start each problem on a new page.
- 6. Show all of your work. No credit will be given for unsupported answers, even if correct.
- 7. Turn in your exam paper with your Blue Book.
- 0. (1 point) Carefully read and complete the instructions at the top of this exam sheet and any additional instructions written on the chalkboard during the exam.
- 1. (6 points) The graph of y = f(x) appears below.



If F'(x) = f(x) for all x and F(0) = 2, then find all values of x for which F(x) = 3.

2. (6 points) Suppose f and g are continuous functions.

- (a) If f is an odd function such that $\int_0^4 f(x) dx = 10$ and $\int_0^5 f(x) dx = 19$, then evaluate $\int_{-4}^5 f(x) dx$. (b) If g is an even function such that $\int_0^4 g(x) dx = 10$ and $\int_0^5 g(x) dx = 19$, then evaluate $\int_{-4}^5 g(x) dx$.
- 3. (10 points) Use the Method of Partial Fractions to evaluate the integral: $\int \frac{2x+1}{(x+1)^2} dx$
- 4. (10 points) Evaluate the indefinite integral: $\int x^2 \sin x \, dx$

- 5. (a) (5 points) Evaluate the following improper integral: $\int_{1}^{2} \frac{1}{\sqrt{2-x}} dx$
 - (b) (5 points) Use the Comparison Test to determine if the improper integral converges or diverges.

$$\int_1^\infty \frac{|\cos x|}{x^2 + 1} \, dx$$

Clearly indicate the function you use for the comparison.

6. The shaded region in the graph is the region in the first quadrant bounded by $y = e^x$ and x = 3.



- (a) (5 points) Set up (but do not evaluate) an integral that gives the volume of the solid of revolution obtained by rotating the shaded region about the x-axis.
- (b) (5 points) Set up (but do not evaluate) an integral that gives the arclength of $y = e^x$ from x = 0 to x = 3.
- (c) (5 points) Set up (but do not evaluate) an integral that gives the area of the shaded region.
- 7. (6 points) Find an **explicit** solution y = f(t) to the initial value problem:

$$\begin{cases} \frac{dy}{dt} = -3y^2 \cos t \\ y(0) = 2 \end{cases}$$

8. (6 points) Determine if the geometric series converges or diverges:

$$\sum_{n=1}^{\infty} \left(\frac{11}{3}\right)^{-n}$$

If it converges, find the sum to which it converges.