

## University of California, San Diego Department of Mathematics

## Instructions

- 1. Write your Name, PID, Section, and Exam Version on the front of your Blue Book.
- 2. No calculators or other electronic devices are allowed during this exam.
- 3. You may use one page of notes, but no books or other assistance during this exam.
- 4. Write your solutions clearly in your Blue Book.
  - (a) Carefully indicate the number and letter of each question and question part.
  - (b) Present your answers in the same order they appear in the exam.
  - (c) Start each problem on a new page.
- 5. Show all of your work. No credit will be given for unsupported answers (even if correct).
- 6. Turn in your exam paper with your Blue Book.
- 0. (1 point) Carefully read and complete the instructions at the top of this exam sheet and any additional instructions written on the chalkboard during the exam.
- 1. (6 points) Let F be the function defined by  $F(x,y) = e^{(x-1)^2+y}$ .
  - (a) Compute algebraically the partial derivatives  $F_x$  and  $F_y$ .
  - (b) What is the equation of the plane tangent to F at the point (1,0)?
- 2. (6 points) A plane is traveling due north with an airspeed of 725 km/hr while descending at a rate of 75 km/hr. There is a 60 km/hr wind blowing from 30 degrees south of due west. What is the ground speed of the airplane?
- 3. (6 points) Let  $f(x,y) = 2x^2 + 3xy + 5y^2$ . At the point (-2,1):
  - (a) Find a unit vector  $\vec{u}$  so that the directional derivative  $f_{\vec{u}}(-2,1)$  is maximum.
  - (b) Find a unit vector  $\vec{u}$  so that the directional derivative  $f_{\vec{u}}(-2,1)$  is minimum.
  - (c) Find a unit vector  $\vec{u}$  so that the directional derivative  $f_{\vec{u}}(-2,1)$  is zero.
- 4. (6 points) Let  $f(x,y) = x^3 + y^2 3x^2 2y + 10$ . Find and critical points and classify each as a local maximum, local minimum, or saddle point.