

Useful Formulas

	Discrete case	Continuous case
$P(a \leq X \leq b)$	$\sum_{i:a \leq x_i \leq b} P(X = x_i)$	$\int_a^b f(x) dx$
$\mu = E[X]$	$\sum_i x_i P(X = x_i)$	$\int_{-\infty}^{\infty} x f(x) dx$
$\text{Var}(X)$	$\sum_i (x_i - \mu)^2 P(X = x_i)$	$\left(\int_{-\infty}^{\infty} x^2 f(x) dx \right) - \mu^2$
$\text{SD}(X)$	$\sqrt{\text{Var}(X)}$	$\sqrt{\text{Var}(X)}$

Distribution	probability function or density	E[X]	SD(X)
Binomial(n, p)	$P(X = k) = \binom{n}{k} p^k (1-p)^{n-k}$ for $k = 0, 1, \dots, n$	np	$\sqrt{np(1-p)}$
Poisson(λ)	$P(X = k) = e^{-\lambda} \lambda^k / k!$ for $k = 0, 1, \dots$	λ	$\sqrt{\lambda}$
Geometric(p)	$P(X = k) = (1-p)^{k-1} p$ for $k = 1, 2, \dots$	$1/p$	$\sqrt{1-p}/p$
Uniform(a, b)	$f(x) = 1/(b-a)$ for $a < x < b$	$(a+b)/2$	$(b-a)/\sqrt{12}$
Exponential(λ)	$f(x) = \lambda e^{-\lambda x}$ for $x > 0$	$1/\lambda$	$1/\lambda$
Normal(μ, σ^2)	$f(x) = (2\pi\sigma^2)^{-1/2} e^{-(x-\mu)^2/2\sigma^2}$	μ	σ

$$E[X + c] = E[X] + c \qquad E[cX] = cE[X] \qquad E[X + Y] = E[X] + E[Y].$$

$$\text{Var}(X + c) = \text{Var}(X) \qquad \text{Var}(cX) = c^2 \text{Var}(X)$$

$\text{Var}(X + Y) = \text{Var}(X) + \text{Var}(Y)$ if X and Y are independent.

$$E[\bar{X}] = \mu \qquad \text{SD}(\bar{X}) = \sigma/\sqrt{n} \qquad E[\hat{p}] = p \qquad \text{SD}(\hat{p}) = \sqrt{\frac{p(1-p)}{n}}$$

$$ME = z^* \sqrt{\frac{\hat{p}(1-\hat{p})}{n}} \qquad Z = \frac{p - p_0}{\sqrt{\frac{p_0(1-p_0)}{n}}}$$