

## Useful Formulas

$$\bar{y} = \frac{1}{n} \sum_{i=1}^n y_i \quad s = \sqrt{\frac{1}{n-1} \sum_{i=1}^n (y_i - \bar{y})^2} \quad r = \frac{1}{n-1} \sum_{i=1}^n \left( \frac{x_i - \bar{x}}{s_x} \right) \left( \frac{y_i - \bar{y}}{s_y} \right)$$

$$\hat{y} = b_0 + b_1 x \quad b_1 = r \frac{s_y}{s_x} \quad b_0 = \bar{y} - b_1 \bar{x}$$

### Discrete Case

$$P(a \leq X \leq b) = \sum_{i: a \leq x_i \leq b} P(X = x_i)$$

$$\mu = E[X] = \sum_i x_i P(X = x_i)$$

$$\sigma^2 = \text{Var}(X) = \sum_i (x_i - \mu)^2 P(X = x_i)$$

### Continuous Case

$$\int_a^b f(x) dx$$

$$\int_{-\infty}^{\infty} x f(x) dx$$

$$\left( \int_{-\infty}^{\infty} x^2 f(x) dx \right) - \mu^2$$

Distribution	Probability Density Function	$E[X]$	$\text{Var}(X)$
Binomial( $n, p$ )	$P(X = k) = \binom{n}{k} p^k (1-p)^{n-k}$ for $k = 0, 1, \dots, n$	$np$	$np(1-p)$
Poisson( $\lambda$ )	$P(X = k) = e^{-\lambda} \lambda^k / k!$ for $k = 0, 1, \dots$	$\lambda$	$\lambda$
Geometric( $p$ )	$P(X = k) = (1-p)^{k-1} p$ for $k = 1, 2, \dots$	$1/p$	$(1-p)/p^2$
Uniform( $a, b$ )	$f(x) = 1/(b-a)$ for $a < x < b$	$(a+b)/2$	$(b-a)^2/12$
Exponential( $\lambda$ )	$f(x) = \lambda e^{-\lambda x}$ for $x > 0$	$1/\lambda$	$1/\lambda^2$
Normal( $\mu, \sigma^2$ )	$f(x) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-(x-\mu)^2/2\sigma^2}$	$\mu$	$\sigma^2$

$$E[\bar{X}] = \mu \quad \text{SD}(\bar{X}) = \frac{\sigma}{\sqrt{n}} \quad E[\hat{p}] = p \quad \text{SD}(\hat{p}) = \sqrt{\frac{p(1-p)}{n}}$$

Test	ME for Interval	Test Statistic	df
One-proportion $z$ -test	$z^* \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$	$Z = \frac{p - p_0}{\sqrt{\frac{p_0(1-p_0)}{n}}}$	N/A
One-sample $t$ -test	$t^* \frac{s}{\sqrt{n}}$	$T = \frac{\bar{X} - \mu_0}{s/\sqrt{n}}$	$n - 1$
Paired $t$ -test	$t^* \frac{s_d}{\sqrt{n}}$	$T = \frac{\bar{d}}{s_d/\sqrt{n}}$	$n - 1$
Two-sample $t$ -test	$t^* \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$	$T = \frac{\bar{X} - \bar{Y}}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$	$\min\{n_1 - 1, n_2 - 1\}$
Regression slope	$t^* \text{SE}(b_1)$	$T = \frac{b_1}{\text{SE}(b_1)}$	$n - 2$