

## University of California, San Diego Department of Mathematics

## Instructions

- 1. Write your Name, PID, Section, and Exam Version on the front of your Blue Book.
- 2. No calculators or other electronic devices are allowed during this exam.
- 3. You may use one page of notes, but no books or other assistance during this exam.
- 4. Read each question carefully, and answer each question completely.
- 5. Write your solutions clearly in your Blue Book.
  - (a) Carefully indicate the number and letter of each question and question part.
  - (b) Present your answers in the same order they appear in the exam.
  - (c) Start each problem on a new page.
- 6. Show all of your work. No credit will be given for unsupported answers, even if correct.
- 7. Turn in your exam paper with your Blue Book.
- 0. (1 point) Carefully read and complete the instructions at the top of this exam sheet and any additional instructions written on the chalkboard during the exam.
- 1. (7 points) Find all solutions to  $z^5 = -5$ . You may leave your answers in polar form.
- 2. (8 points) Evaluate the indefinite integral:

$$\int \frac{2x+3}{x^2(x^2+1)} \, dx.$$

3. (8 points) Evaluate the indefinite integral:

$$\int \frac{1}{(4x^2 + 25)^2} \, dx.$$

4. (8 points) Evaluate the improper integral and determine if it converges or diverges:

$$\int_{-\infty}^{0} xe^{-x^2} dx$$

5. (8 points) Determine if the improper integral converges. You do not need to evaluate it, but you must explain how you know it converges or diverges:

$$\int_0^\infty e^{-(3x^2 + 2x + 1)} \, dx$$