1. (50 points) Check all the correct statements.
   □ The number of different strings you can get by reordering letters in the word aabbc is 30.
   □ There are 25 different strings of length 5 over the alphabet with two letters.
   □ If you have 26 balls in 5 boxes, then there is a box with at least 6 balls.
   □ There are 6 different surjective functions from [3] to [2].
   □ There are 15 variants to put 4 identical balls into 3 different boxes.

2. (10 points) Let us assume that we are given $\ell$ lines that are not parallel to each other. Prove that there are at least two of them such that angle between them is at most $\pi/\ell$. 
3. (10 points) Prove that for all integers $n > 0$, the sum $\frac{1}{1^2} + \frac{1}{2^2} + \cdots + \frac{1}{n^2}$ is at most 2.
4. (10 points) Find a closed formula (no summation signs) for the expression \( \sum_{i=1}^{n} i^2 \binom{n}{i} (-1)^i \).
5. (10 points) Find a closed formula (no summation signs) for the expression $S(n, n - 2)$. 