

Math 10B. Lecture Examples.

Section 5.2. The definite integral[†]

Example 1 Use the formula for the area of a triangle to evaluate $\int_{-3}^3 (x+1) dx$.

Answer: Figure A1 • $\int_{-3}^3 (x+1) dx = 6$.

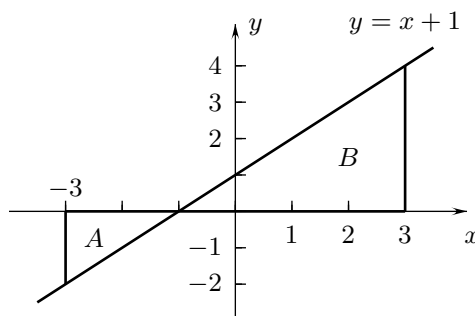


Figure A1

Example 2 Calculate the right Riemann sum for $\int_0^1 x^2 dx$ corresponding to the partition of $[0,1]$ into five equal subintervals. Draw the curve $y = x^2$ with the rectangles whose areas give the Riemann sum.

Answer: Figure A2 • [Right Riemann sum] = 0.44

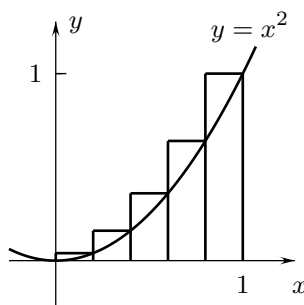


Figure A2

[†]Lecture notes to accompany Section 5.2 of *Calculus* by Hughes-Hallett et al.

Example 3 Use the fact that the curve $y = \sqrt{16 - x^2}$ is the upper half of the circle $x^2 + y^2 = 16$ of radius 4 to find the exact value of $\int_{-4}^0 \sqrt{16 - x^2} dx$.

Answer: Figure A3 • $\int_{-4}^0 \sqrt{16 - x^2} dx = 4\pi$

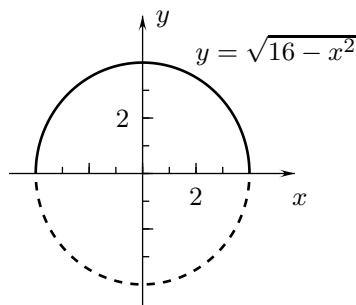


Figure A3

Example 4 Use five rectangles of equal width to find the approximate value of $\int_0^{50} H(x) dx$ for the function $y = H(x)$ of Figure 1.

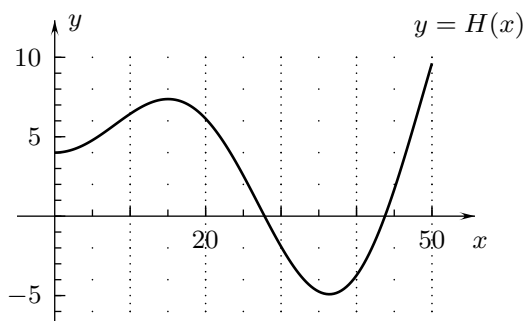


FIGURE 1

Answer: One answer: Figure A4 • $\int_0^{50} H(x) dx \approx (5 + 7 + 2.5 - 5 + 4)(10) = 135$

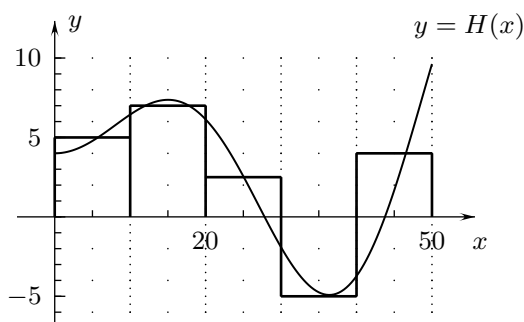


Figure A4

Interactive Examples

Work the following Interactive Examples on Shenk's web page, <http://www.math.ucsd.edu/~ashenk/>.[‡]

Section 6.2: 1–4

[‡]The chapter and section numbers on Shenk's web site refer to his calculus manuscript and not to the chapters and sections of the textbook for the course.