Math 10B. Lecture Examples.

Section 5.4. Theorems about definite integrals^{\dagger}

Example 1 What is the integral of g from 1 to 8 if its integral from 1 to 5 is -7 and its integral from 5 to 8 is 9?

Answer:
$$\int_{1}^{8} g(x) dx = 2$$
Example 2 What is
$$\int_{-35}^{35} [2\mathbf{p}(\mathbf{x}) - 3\mathbf{q}(\mathbf{x})] d\mathbf{x}$$
 if
$$\int_{-35}^{35} \mathbf{p}(\mathbf{x}) d\mathbf{x} = 10$$
 and
$$\int_{-35}^{35} \mathbf{q}(\mathbf{x}) d\mathbf{x} = 20$$
?
Answer:
$$\int_{-35}^{35} [2p(x) - 3q(x)] dx = -40$$
Example 3 What is
$$\int_{3}^{0} \mathbf{Y}(\mathbf{x}) d\mathbf{x}$$
 if
$$\int_{0}^{4} \mathbf{Y}(\mathbf{x}) d\mathbf{x} = 100$$
 and
$$\int_{4}^{3} \mathbf{Y}(\mathbf{x}) d\mathbf{x} = -25$$
?
Answer:
$$\int_{3}^{0} Y(x) dx = -75$$
Example 4 What is
$$\int_{0}^{3} [2\mathbf{f}(\mathbf{x}) - 4\mathbf{g}(\mathbf{x})] d\mathbf{x}$$
 if
$$\int_{0}^{3} \mathbf{f}(\mathbf{x}) d\mathbf{x} = 100$$
 and
$$\int_{0}^{3} \mathbf{g}(\mathbf{x}) d\mathbf{x} = 200$$
?
Answer:
$$\int_{0}^{3} [2f(x) - 4g(x)] d\mathbf{x}$$
 if
$$\int_{0}^{3} \mathbf{f}(\mathbf{x}) d\mathbf{x} = 100$$
 and
$$\int_{0}^{3} \mathbf{g}(\mathbf{x}) d\mathbf{x} = 200$$
?
Example 5 Use the formulas for areas of rectangles and circles to evaluate

$$\int_0^2 (5 - 3\sqrt{4 - x^2}) \, \mathrm{d}x.$$
Answer: $\int_0^2 (5 - 3\sqrt{4 - x^2}) \, \mathrm{d}x = 10 - 3\pi$

Interactive Examples

Work the following Interactive Examples on Shenk's web page, http://www.math.ucsd.edu/~ashenk/:[‡] Section 6.2: Example 6

[†]Lecture notes to accompany Section 5.4 of *Calculus* by Hughes-Hallett et al.

 $^{^{\}ddagger}$ The chapter and section numbers on Shenk's web site refer to his calculus manuscript and not to the chapters and sections of the textbook for the course.