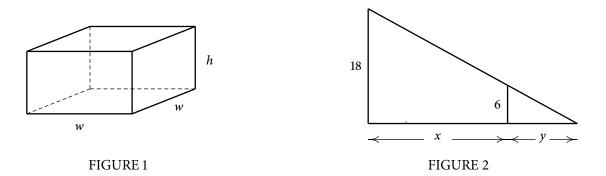
Name

Work alone and use no books, notes, or calculators. Show your work with your answers on 8.5"×11" *paper and staple the pages to the exam when you turn them in. Justify your conclusions.*

- **Problem 1** (15 points) Find the derivatives (a) y'(x) for $y(x) = \ln(x^3 + x^2)$, (b) $\frac{d}{dx}(\cos^2 x)$, and (c) f'(2) for $f(x) = \tan^{-1} x$ (the inverse tangent function).
- **Problem** 2 (10 points) Give an equation of the tangent line to $y = \sqrt{x^2 + 9}$ at x = 4.
- **Problem 3** (10 points) At a particular moment on a trip you are driving 60 miles per hour and your car is using gas at the rate of $\frac{1}{20}$ gallons per mile. At what rate are you using gasoline, measured in gallons per hour?
- **Problem 4** (10 points) A rectangular box with a square base and no top, as in Figure 1, is to be constructed to have a volume of $\frac{1}{2}$ cubic foot. Find the dimensions of the box that requires the least amount of material for the bottom and four sides.



- Problem 5 A six-foot-tall man is walking away from an eighteen-foot-high post with a lamp at its top (Figure 2). (a) (5 points) Find an equation relating his distance x from the post and the length y of his shadow. (b) (5 points) How fast is his shadow growing if he is walking two miles per hour?
- **Problem 6** (10 points) What is the rate of change of the width of a cube with respect to time at a moment when it is two inches wide and its volume is increasing 36 cubic inches per minute? ($V = w^3$)
- *Problem* 7 (a) (3 points) Find the limits of f(x) = x³ 3x² + 4 as x → ±∞. (b) (4 points) Find the open intervals on which f is increasing and decreasing and its local and global maxima and minima.
 (c) (4 points) Find the open intervals on which the graph of f is concave up and concave down and the inflection points of the graph. (d) (4 points) Draw the graph of f.

Problem 8 (10 points) Find (a) $\lim_{x \to \pi} \left(\frac{\sin x}{\sin(2x)} \right)$ and (b) $\lim_{x \to \infty} \left(\frac{\ln x}{x^2 + 1} \right)$. Scores: 1 2 3 4 5 6 7 8 Total