Math 20C. Lecture Examples.

Section 12.1. Vectors in the plane^{\dagger}

Example 1 Find the x- and y-components of the vector u of length 10 with angle of inclination $\frac{5}{6}\pi$.

Answer: Figure A1a • $\mathbf{u} = \langle -5\sqrt{3}, 5 \rangle$ • Figure A1b









[†]Lecture notes to accompany Section 12.1 of Calculus, Early Transcendentals by Rogawski.

Answer: (a) $\mathbf{v} + \mathbf{w} = \langle 5, 4 \rangle \bullet$ Figure A3a (b) $\mathbf{w} - \mathbf{v} = \langle -3, 2 \rangle \bullet$ Figure A3b







FIGURE 1

Answer: S = (16, 6)

Example 6 Give the unit vector $\mathbf{e}_{\mathbf{v}}$ and the vector \mathbf{w} of length 5 with the same direction as $\mathbf{v} = \langle -3, 2 \rangle$.

Answer:
$$\mathbf{e}_{\mathbf{v}} = \frac{\langle -3, 2 \rangle}{\sqrt{13}} \bullet \mathbf{w} = \frac{\langle -15, 10 \rangle}{\sqrt{13}}$$

Example 7 Express 3(4i - j) - 2(10i - 5j) in the form ai + bj. Answer: 3(4i - j) - 2(10i - 5j) = -8i + 7j. (Example 4 is the same calculation with different notation.)

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Example 8 One man is lifting a boulder with a rod while another is pulling it with a rope as in Figure 2. (a) Find the x- and y-components of the two force vectors, with the usual orientation of axes. (b) Find the resultant of the two forces and the approximate decimal values of its magnitude and angle of inclination



FIGURE 2

Answer: (a) [Force exerted by the man with the rod] = $\mathbf{F} = 300 \left\langle \cos\left(\frac{7}{18}\pi\right), \sin\left(\frac{7}{18}\pi\right) \right\rangle$ pounds. • [Force exerted by the man with the rope] = $\mathbf{G} = 150 \left\langle \cos\left(\frac{1}{9}\pi\right), \sin\left(\frac{1}{9}\pi\right) \right\rangle$ pounds. (b) [Resultant] = $\left\langle 300 \cos\left(\frac{7}{18}\pi\right) + 150 \cos\left(\frac{1}{9}\pi\right), 300 \sin\left(\frac{7}{18}\pi\right) + 150 \sin\left(\frac{1}{9}\pi\right) \right\rangle \doteq \left\langle 244, 333 \right\rangle$ pounds • [Magnitude of the combined force $\doteq 413$ pounds • [Angle of inclination] $\doteq \tan^{-1}\left(\frac{333}{244}\right) \doteq 0.94$ radians.

Interactive Examples

Work the following Interactive Examples on Shenk's web page, http//www.math.ucsd.edu/~ashenk/:[‡] Section 12.1: Examples 1, 6, 7

 $[\]ddagger$ The chapter and section numbers on Shenk's web site refer to his calculus manuscript and not to the chapters and sections of the textbook for the course.