## REMEMBER THIS EXAM IS GRADED BY A HUMAN BEING. WRITE YOUR SOLUTIONS NEATLY AND COHERENTLY, OR THEY RISK NOT RECEIVING FULL CREDIT.

IF YOU DO NOT ASSIGN THE PAGES OF YOUR WORK TO THE QUESTIONS OF THE EXAM IN YOUR UPLOAD TO GRADESCOPE, YOU WILL LOSE POINTS (1 POINT FOR EVERY QUESTION THAT YOU FAIL TO ASSIGN THE PAGES TO).

[^0]| FROM THE MOMENT YOU ACCESS THE |
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| MIDTERM ON GRADESCOPE, YOU WILL HAVE |
| A TOTAL OF 70 MINUTES TO COMPLETE AND |
| UPLOAD YOUR SOLUTIONS TO GRADESCOPE. |
| THE EXAM IS WRITTEN TO TAKE 50 MIN- |
| UTES. IT IS YOUR RESPONSIBILITY TO UP- |
| LOAD YOUR SOLUTIONS ON TIME. |

> THE MIDTERM IS OPEN TEXTBOOK, AND YOU CAN REWATCH LECTURES AND REVIEW THE LECTURE SLIDES. YOU ARE NOT ALLOWED TO USE CALCULATORS, COMPUTER ALGEBRA SYSTEMS, OR SIMILAR SOFTWARE. YOU ARE NOT ALLOWED TO CONSULT OTHER PEOPLE OR RESOURCES ON THE INTERNET. IN PARTICULAR, CONTRACT CHEATING AND OTHER INSTANCES OF ACADEMIC DISHONESTY CAN RESULT IN SUSPENSION OR DISMISSAL.

| THIS EXAM IS PROPERTY OF THE REGENTS |
| :--- |
| OF THE UNIVERSITY OF CALIFORNIA AND |
| NOT MEANT FOR OUTSIDE DISTRIBUTION. |
| IF YOU SEE THIS EXAN APPEARING ELSE- |
| WHERE, PLEASE NOTIFY THE INSTRUCTOR AT |
| BAUQUCSD.EDU AND THE UCSD OFFICE OF |
| ACADEMIC INTEGRITY AT AIO@UCSD.EDU. |

## EXCEL WITH INTEGRITY PLEDGE

I pledge to be fair to my classmates and instructors by completing all of my academic work with integrity. This means that I will respect the standards set by the instructor and institution, be responsible for the consequences of my choices, honestly represent my knowledge and abilities, and be a community member that others can trust to do the right thing even when no one is watching. I will always put learning before grades, and integrity before performance. I pledge to excel with integrity.

In addition to the above, I pledge that I did not receive outside assistance with this exam. Outside assistance includes but is not limited to other people, the internet, and resources beyond the textbook, lecture notes/videos, and homework assignments.

To acknowledge that you agree to this pledge, you must copy the sentence:
I choose to excel with integrity as a member of the University of California, San Diego.
Make sure to sign your name below it and date it as well. Exams without this pledge will not be graded.

1. Suppose that the time it takes for you to complete your probability homework is distributed according to an exponential random variable with mean 1 hour. You start your homework at 8:00 PM. Your bedtime is 10:00 PM. If you finish your homework before your bedtime, you watch TV until your bedtime and then go to sleep. If you do not finish by your bedtime, you go to sleep anyway, and so you do not watch TV at all. Let $Y$ be the random variable that measures the amount of time in hours that you spend watching TV.
(a) Calculate the CDF of $Y$.
(b) Calculate the expected value $\mathbb{E}[Y]$.
2. Let $X \sim \operatorname{Poisson}(\lambda)$. Compute

$$
\mathbb{E}\left[\frac{1}{1+X}\right]
$$

3. Suppose that we plan to interview $n$ randomly chosen individuals to estimate the unknown fraction $p \in(0,1)$ of the population that likes ice cream. Let $\hat{p}=\frac{S_{n}}{n}$ be the random variable that records the proportion of the individuals who say they do like ice cream. How many people must we interview to have at least a $95 \%$ chance of capturing the true fraction $p$ with a margin of error .01? You may leave your answer in terms of the inverse $\Phi^{-1}$ of the CDF of the standard normal.
4. Suppose that the random variable $X$ has p.d.f.

$$
f(x)=\frac{\lambda}{2} e^{-\lambda|x|}
$$

where $\lambda>0$.
(a) Compute the moment generating function $M_{X}(t)$ of $X$.
(b) Use the moment generating function to compute the $n$th moment of $X$.


[^0]:    WRITE YOUR NAME AND STUDENT ID ON THE FIRST PAGE OF YOUR UPLOAD
    WRITE YOUR SOLUTIONS TO EACH PROBLEM ON SEPARATE PAGES. CLEARLY INDICATE AT THE TOP OF EACH PAGE THE NUMBER OF THE CORRESPONDING PROBLEM. DIFFERENT PARTS OF THE SAME PROBLEM CAN BE WRITTEN ON THE SAME PAGE (FOR EXAMPLE, PART (A) AND PART (B)).

