

## §12.1-12.4

### §12.1

- Functions of two variables: plugging in numbers into a function and reading a table of values for a function.
- Plotting points in 3 space.
- The distance formula.

### §12.2-12.3

- The graph of a function  $f$ . I.e. the set of points in three space of the form  $(a, b, f(a, b))$ .
- Cross sections and level curves of a function. Know how to use these to help graph a function of two variables.
- Contour maps (also called contour diagrams).

### §12.4

- Linear functions.
- Graphs of linear functions are planes.

## §13.1-13.4:

### §13.1:

- Vectors in 2 and 3 dimensions. Displacement vectors between two points.
- Magnitude (length) of vectors.
- The component vectors  $\vec{i}, \vec{j}, \vec{k}$ .
- Addition, scalar multiplication, subtraction. Understand how do these operations using components, and what they mean geometrically.

- What does it mean for vectors to be parallel? Perpendicular?
- Unit vectors.

### §13.2

- Word problems.
- Writing vectors in two dimensions in “polar form”. I.e.  $\vec{v} = \langle r \cos \theta, r \sin \theta \rangle$  where  $r = \|\vec{v}\|$  and  $\theta$  is the angle  $\vec{v}$  makes with the positive  $x$ -axis.

### §13.3

- The dot product. In particular, the “algebraic definition” and the “geometric definition”.
- Using the dot product to find the angle between two vectors. In particular, two vectors are perpendicular if and only if their dot product is zero.
- Finding the equation of a plane if you know a point on the plane and a vector orthogonal to the plane.
- Projections. I.e. given two vectors  $\vec{v}$  and  $\vec{w}$ , write  $\vec{v} = proj_{\vec{w}}(\vec{v}) + \vec{v}_{\perp}$  where  $\vec{v}_{\perp}$  is perpendicular to  $\vec{w}$  and  $proj_{\vec{w}}(\vec{v})$  is parallel to  $proj_{\vec{w}}(\vec{w})$ .

### §13.4

- The cross product. In particular, the “algebraic definition” and the “geometric definition”.
- Properties of the cross product.
- Using the cross product to find a normal vector to a plane.
- Using the cross product to compute the area of the parallelogram spanned by two vectors.