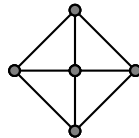


## HOMWORK 9 - MATH 100A - DUE FRIDAY DECEMBER 8TH

In this homework assignment you don't need to prove anything. Just find the correct answer!



Use the above graph in Problems 1-5.

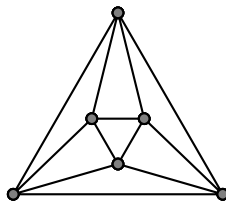
**Problem 1.** Let  $\Gamma = (V, E)$  be the above set of edges and vertices. Compute  $|\text{Aut}(\Gamma)|$ .

**Problem 2.** Consider the action of  $\text{Aut}(\Gamma)$  on the vertices  $V$ . How many orbits are there?

**Problem 3.** Consider the action of  $\text{Aut}(\Gamma)$  on the edges,  $E$ . How many orbits are there?

**Problem 4.** Count the number of colorings of the vertices with  $k$  not necessarily distinct colors, up to symmetry.

**Problem 5.** Count the number of colorings of the edges with  $k$ -colors, up to symmetry.



Use the above graph in Problems 6 & 7.

**Problem 6.** Let  $\Gamma = (V, E)$  be the above graph. Consider the action of  $\text{Aut}(\Gamma)$  on the vertices. How many orbits are there?

**Problem 7.** Choose a vertex  $v \in V$  and compute the size of  $\text{Orb}(v)$  and  $\text{Stab}(v)$ . Use these results to compute  $|\text{Aut}(\Gamma)|$ .



Use the above graph in problems 8 & 9.

**Problem 8.** Let  $\Gamma = (V, E)$  be the above graph. Compute  $|\text{Aut}(\Gamma)|$ .

**Problem 9.** Count the number of colorings of the vertices of  $\Gamma$  with  $k$  not necessarily distinct colors, up to symmetry.