

(Example 4.32)

Animals of the forest need to cross a remote highway. From experience they know that, from the moment someone arrives at the roadside, the time till the next car is an exponential random variable with expected value **30 minutes**. The turtle needs **10 minutes** to cross the road.

- (a) What is the probability that the turtle can cross the road safely?
- (b) Now suppose that when the turtle arrives at the roadside, the fox tells her that he has been there already **5 minutes** without seeing a car go by. What is the probability now that the turtle can cross safely?

Write $X =$ time to next car

$$E(X) \sim 30 = 1/\lambda \Rightarrow \lambda = 1/30 \quad \text{"1 30th cars per minute"}$$

$$\Rightarrow X \sim \text{Exp}(1/30)$$

$$(a) P(X > 10) = 1 - P(X \leq 10) = 1 - F_X(10) \\ = 1 - (1 - e^{-t/30}) = \boxed{e^{-1/3}} \approx .72$$

$$(b) P(X > \overset{5+10}{\cancel{5}} | X > 5) = P(X > 10) \quad \text{by the memoryless property} \\ = e^{-1/3}$$