Math 20A
Midterm Exam 1
October 23, 2012
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Version A

Instructions

1. **No calculators or other electronic devices are allowed during this exam.**
2. **You may use one page of notes, but no books or other assistance during this exam.**
3. **Write your *Name*, *PID*, and *Section* on the front of your Blue Book.**
4. **Write the *Version* of your exam at the top of the page on the front of your Blue Book.**
5. **Write your solutions clearly in your Blue Book**

    (a) **Carefully indicate the number and letter of each question and question part.**
    (b) **Present your answers in the same order they appear in the exam.**
    (c) **Start each question on a new side of a page.**

6. **Read each question carefully, and answer each question completely.**
7. **Show all of your work; no credit will be given for unsupported answers.**

0. (1 point) Carefully read and complete the instructions at the top of this exam sheet and any additional instructions written on the chalkboard.

1. (6 points) Evaluate each of the following limits.

    (a) $\lim\limits_{x \to 0} \dfrac{1}{x} \left(\dfrac{1}{x+3} - \dfrac{1}{3} \right)$

    (b) $\lim\limits_{x \to \infty} \sqrt{x+2} - 2\sqrt{x}$

2. (6 points) Let f be a differentiable function. Let $f(1) = 3$, $f'(1) = -2$, $f(2) = -3$, $f'(2) = 1$, $f(3) = 1$, and $f'(3) = 0$

    (a) Find the equation for the tangent line to $y = f(x)$ at $x = 2$.

    (b) Determine which intervals on which $f(x) = 0$ has a solution. Justify your answer with appropriate theorems.

3. (9 points) For each of the following functions $f(x)$, compute its derivative $f'(x)$:

    (a) $f(x) = x^2 e^x$.

    (b) $f(x) = \dfrac{x^5 - e^x}{5x + 1}$.

    (c) $f(x) = \pi^3(x + 1)$.

Note: Problem 4 is on the other side of this page.

4. (6 points) Let

$$f(x) = \begin{cases} 0 & \text{if } x = 0, \\ x^2 \sin(\frac{1}{x}) & \text{if } x \neq 0. \end{cases}$$

(a) Express $f'(0)$ as a limit.

(b) Evaluate $f'(0)$ using the Squeeze Theorem.