Homework 4

**Note:** The score you earn will be based on the correctness of your solutions. A "right answer" will earn no credit without a correct solution to support it.

- (6 points) 1. Consider the circle C of radius 2, centered at the origin (0,0).
  - (a) Find a parametrization for C inducing a counterclockwise orientation and starting at (2, 0).
  - (b) Find a parametrization for C if it is now centered at the point (4,7).
- (6 points) 2. The position vector for a particle moving on a helix is

$$\mathbf{c}(t) = \left(\cos\left(t\right), \sin\left(t\right), t^{2}\right).$$

- (a) Find the speed of the particle at time  $t_0 = 4\pi$ .
- (b) Find a parametrization for the tangent line to  $\mathbf{c}(t)$  at  $t_0 = 4\pi$ .
- (c) Where will this line intersect the xy-plane?
- (6 points) 3. Find  $\frac{\partial}{\partial s} (f \circ T) (1, 0)$ , where  $f(u, v) = \cos(u) \sin(v)$  and  $T : \mathbb{R}^2 \to \mathbb{R}^2$  is defined by  $T(s, t) = \left(\cos\left(t^2 s\right), \log\left(\sqrt{1+s^2}\right)\right).$
- (6 points) 4. Let  $g(u, v) = (e^u, u + \sin(v))$  and f(x, y, z) = (xy, yz). Compute  $\mathbf{D}(g \circ f)$  at (0, 1, 0) using the chain rule.
- (6 points) 5. Find the plane plane tangent to each of the following surfaces at the indicated point on the surface:
  - (a) the surface  $x^2 + 2y^2 + 3xz = 10$  at the point  $\left(1, 2, \frac{1}{3}\right)$
  - (b) the surface  $y^2 x^2 = 3$  at the point (1, 2, 8)
- (6 points) 6. Find a unit normal vector to the surface  $\cos(xy) = e^z 2$  at the point  $(1, \pi, 0)$ .