MATH 170C PROJECT 2

(1) Write a MATLAB routine to solve a two-point boundary-value problem,

$$y'' = f(t, y, y'), \qquad y(a) = \alpha, \qquad y(b) = \beta,$$

using the shooting method where the underlying one-step method is the explicit fourth-order Runge–Kutta method. You will need to extend the RK4 method that you developed for Project 1 so that it can be used on systems of first-order ordinary differential equations.

For the root-finding for the initial velocity, use either the secant method or the Newton method with the complex-step derivative approximation, with error tolerance `TOL`, and maximum number of iterations `MaxIters`.

The resulting function should be written so that it can be called in MATLAB by typing:

```
[x,t]=BVP_shooting(@f,a,b,alpha,beta,h,TOL,MaxIters)
```

Then, use your method to solve the following two-point boundary-value problem,

$$y'' = e^t + y\cos t - (t+1)y', \qquad y(0) = 1, \qquad y(1) = 3,$$

for $h = 0.1$, $h = 0.05$.

(2) Write a MATLAB routine to solve linear two-point boundary-value problem,

$$y'' = u + vx + wy', \qquad y(a) = \alpha, \qquad y(b) = \beta,$$

using the finite-difference method. The resulting function should be written so that it can be called in MATLAB by typing:

```
[x,t]=BVP_finitediff(@u,@v,@w,a,b,alpha,beta,h)
```

You may use the built-in MATLAB routines to perform the matrix inverse. Apply your method to the same example problem as in Problem 1, and compare your results.