

Name: \_\_\_\_\_ PID: \_\_\_\_\_

TA: \_\_\_\_\_ Sec. No: \_\_\_\_\_ Sec. Time: \_\_\_\_\_

Math 20C

Midterm Exam 2 (blue)

May 21, 2008

*Turn off and put away your cell phone.*

*No calculators or any other devices are allowed on this exam.*

*You may use one page of notes, but no books or other assistance on this exam.*

*Read each question carefully, answer each question completely, and show all of your work.*

*Write your solutions clearly and legibly; no credit will be given for illegible solutions.*

*If necessary, write "see other side" and continue working on the back of the same sheet.*

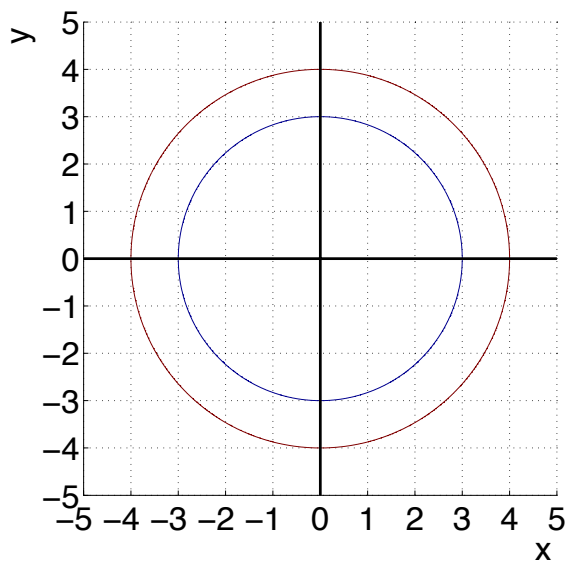
*If any question is not clear, ask for clarification.*

#	Points	Score
1	6	
2	9	
3	6	
4	6	
$\Sigma$	27	

1. Let  $z = f(x, y) = x^2 + y^2 + 800$ .

(a) (3 points) Compute  $\frac{\partial}{\partial x} (f(x, y)^{100})$ .

(b) (3 points) Two contours  $f(x, y) = k$  are shown on this plot. Label each contour with its value of  $k$ . The grid lines are shown to help you read off coordinates that may be useful in doing this computation.



2. Let  $f(x, y) = x^2 - xy - 3y + 40$ .

(a) (3 points) Find the directional derivative of  $f$  at the point  $(2, 4)$  in the direction towards the point  $(6, 1)$ .

(b) (6 points) Find all critical points of  $f$ . Classify each critical point as a local maximum, local minimum, or saddle point. Compute the value of  $f$  at each critical point.

3. Let  $f(x, y) = x^2y^3 + 20$ .

(a) (4 points) Find an equation for the tangent plane to the surface  $z = f(x, y)$  at the point where  $x = 3$  and  $y = -1$ .

(b) (2 points) Use the linear approximation to  $f(x, y)$  at  $(3, -1)$  to estimate the value of  $f(3.1, -1.2)$ . *Hint: This makes use of your answer to (a) and is not the exact value of  $f(3.1, -1.2)$ .*

4. The temperature at a point  $(x, y)$  is  $T(x, y)$ , measured in degrees Celsius, and satisfies  $T_x(2, 3) = 8$  and  $T_y(2, 3) = 6$ . A scarab beetle crawls so that its position after  $t$  seconds is given by  $x = \sqrt{2+t}$ ,  $y = 2 + \frac{1}{2}t$ , where  $x$  and  $y$  are measured in centimeters.

(a) (3 points) How fast is the temperature rising on the beetle's path after 2 seconds?

(b) (3 points) In what direction from the point  $(2, 3)$  does the temperature *decrease* the fastest? Express your answer as a unit vector.

Did you remember to:

- Fill out your name, student ID number, and TA and section information on the front?
- Check your work?

Exam booklets will be collected promptly when time is called.